

Properties of Logarithms

Exponential Form

$$b^y = x$$

Transforms in both directions

$$\leftrightarrow$$

Logarithmic Form

$$y = \log_b x$$

Rules: $x > 0$, $b > 0$, $b \neq 1$

and $\log_b u = \log_b v$ if and only if $u = v$

$\log_b nk = \log_b n + \log_b k$	<p><u>Product Rule:</u> The log of the product of two numbers is equal to the <u>sum</u> of the log of each of the numbers.</p>
$\log_b \frac{n}{k} = \log_b n - \log_b k$	<p><u>Quotient Rule:</u> The log of the quotient of two numbers is equal to the <u>difference</u> between the log of each number.</p>
$\log_b n^k = k \log_b n$	<p><u>Power Rule:</u> The log of a number that is raised to a power is equal to the exponent <u>times</u> the log of the number.</p>
$\log x = \log_{10} x$	<p><u>Definition:</u> The word “log” with no base shown is a shorthand way of writing a log with the base of 10. This is called a <u>Common Log</u>.</p>
$\ln x = \log_e x$	<p><u>Definition:</u> The symbol “ln” is a shorthand way of writing a log with the base of e. This is called a <u>Natural Log</u>.</p>
$\log_b 1 = 0$	<p>The log of 1 equals zero because if we go back to exponential form, we see that $b^0 = 1$ ($b \neq 0$) (see definition of zero exponent)</p>
$\log_b b = 1$	<p>The log of b to the base b equals 1 because if we go back to exponential form, we see that $b^1 = b$ ($b \neq 0$)</p>
$\log_b b^x = x$	<p>The log of b^x to the base b is equal to just the exponent x because if we go back to exponential form, we see that $b^x = b^x$ ($b \neq 0$)</p>
$b^{\log_b x} = x$	<p>A base b raised to the power of a log to that same base is equal to just the argument x because if we go into logarithmic form, we see that $\log_b x = \log_b x$ ($b \neq 0$)</p>
$\log_b x = \frac{\log x}{\log b} = \frac{\ln x}{\ln b}$	<p><u>Change of Base Theorem:</u> Allows you to find the value of a logarithm with a base other than 10 or e using your calculator (use either of the fractions shown)</p>