

Sets

A set is a collection of well-defined objects.

Methods for Describing Sets	Definition	Example
Word Description	An accurate description of the set.	The set of Natural numbers less than 9.
Roster	A list of elements inside braces.	$A = \{1, 2, 3, 4, 5, 6, 7, 8\}$
Set Builder	Shorthand used to write sets.	$A = \{x \in \mathbb{N} \mid x < 9\}$ This read as: The set of all x's element of natural numbers, such that x less than 9.

Symbol	Name	Definition	Example	Remark
\emptyset or $\{ \}$	Empty Set or Null Set	The set that contains no elements.	$A = \{ \}$ $A = \emptyset$	The \emptyset symbol should not be confused with 0. \emptyset is a set which has no elements. 0 is an element that has no value.
U	Universal Set	The set of all elements for a discussion or problem.	$U = \{ \text{All students who come to the Learning \& Tutoring Center for tutoring.} \}$	U set includes students who come to the LTC for any reason.
A'	Complement of Set A	The set of all objects in the universal set but not in set A.	$U = \{2, 3, 4, 5, 6, 7\}$ $A = \{1, 3, 5\}$ $A' = \{2, 4, 6, 7\}$	The complement of set A is $A' = \{2, 4, 6, 7\}$
\in	Element of	This is used to indicate that an element is part of a set.	$B = \{0, 1, 5, 6, 9\}$ $5 \in B$	Read as: 5 is an element in set B.
\notin	Not an element of	This is used to indicate that an element is not a part of a set.	$B = \{0, 1, 5, 6, 9\}$ $2 \notin B$	Read as: 2 is not an element in set B.
$n(A)$	Cardinal Number	The number of distinct elements in set A.	$A = \{a, d, e, g, h\}$ $n(A) = 5$	Read as: n of A equals 5.
$n(A) = n(B)$	Equivalent sets	The cardinal number of elements in Set A and Set B is the same.	$A = \{a, b, d, g, h\}$ $B = \{0, 1, 3, 5, 7\}$ $n(A) = n(B) = 5$	$n(A) = 5$ $n(B) = 5$ $n(A) = n(B) = 5$
$A = B$	Set equality	Set A and Set B	$A = \{2, 4, 7, 8, 9\}$	Equal sets have exactly the

		contain the same elements regardless of order or possible repetition of elements.	$B = \{4, 7, 2, 9, 8\}$ $A = B$	same elements, while equivalent sets have the same number of elements.
$A \subseteq B$	Subset	Every element in Set A is also an element in Set B.	$A = \{a, b, c\}$ $B = \{a, c, b, d, e\}$ $A \subseteq B.$	Read as: Set A is a subset of set B.
$A \subset B$	Proper subset	Every element in Set A is also in Set B. The number of elements in Set A is not equal to the number in Set B.	$A = \{1, 2, 3\}$ $B = \{2, 4, 1, 3, 7\}$ $A \subset B$	Read as: Set A is a proper subset to Set B.
$A \cap B$	Intersection	The set of elements common to both Set A and Set B.	$A = \{1, 2, 3, 4\}$ $B = \{2, 4, 6, 8\}$ $A \cap B = \{2, 4\}$	2 and 4 are common elements to Set A and Set B.
$A \cup B$	Union	The set of elements belong to either set A or set B.	$A = \{1, 2, 3, 4, 5\}$ $B = \{-1, 0, 1, 2, 3\}$ $A \cup B = \{-1, 0, 1, 2, 3, 4, 5\}.$	
$A - B$ or $A \setminus B$	Set difference	The set of elements belong to Set A but not Set B.	$A = \{1, 2, 3, 4, 5, 6\}$ $B = \{2, 4, 6, 8, 10\}$ $A - B$ or $A \setminus B = \{1, 3, 5\}$	
\mathbb{N}	Set of Natural Numbers	The set of counting numbers.	$\mathbb{N} = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, \dots\}$	Set of Natural Numbers contains only positive numbers and could not be decimals, fractions and 0.
\mathbb{W}	Set of Whole Numbers	The set of whole numbers is the set of natural numbers and 0.	$\mathbb{W} = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, \dots\}$	
\mathbb{I} or \mathbb{Z}	Set of Integer Numbers	The set of whole numbers, 0, and negative numbers.	$\mathbb{I} = \{\dots, -4, -3, -2, -1, 0, 1, 2, 3, \dots\}$	

Note: A set with n elements has 2^n subsets and $2^n - 1$ proper subsets.