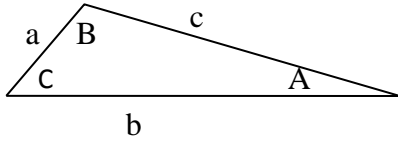


Trigonometric Identities and Formulas

<p>Reciprocal Identities</p> $\csc x = \frac{1}{\sin x} \qquad \sin x = \frac{1}{\csc x}$ $\sec x = \frac{1}{\cos x} \qquad \cos x = \frac{1}{\sec x}$ $\cot x = \frac{1}{\tan x} \qquad \tan x = \frac{1}{\cot x}$ $\cot x = \frac{\cos x}{\sin x} \qquad \tan x = \frac{\sin x}{\cos x}$	<p>Sum and Difference Identities</p> $\sin(x+y) = \sin x \cos y + \cos x \sin y$ $\sin(x-y) = \sin x \cos y - \cos x \sin y$ $\cos(x+y) = \cos x \cos y - \sin x \sin y$ $\cos(x-y) = \cos x \cos y + \sin x \sin y$ $\tan(x+y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$ $\tan(x-y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$
<p>Pythagorean Identities</p> $\sin^2 x + \cos^2 x = 1$ $1 + \tan^2 x = \sec^2 x$ $1 + \cot^2 x = \csc^2 x$	<p>Even-Odd Identities</p> $\sin(-x) = -\sin x$ $\cos(-x) = \cos x$ $\tan(-x) = -\tan(x)$
<p>Double Angle Formulas</p> $\sin 2x = 2\sin x \cos x$ $\cos 2x = \cos^2 x - \sin^2 x$ $= 1 - 2\sin^2 x$ $= 2\cos^2 x - 1$ $\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$	<p>Half Angle Formulas</p> $\sin\left(\frac{x}{2}\right) = \pm \sqrt{\frac{1 - \cos x}{2}}$ $\cos\left(\frac{x}{2}\right) = \pm \sqrt{\frac{1 + \cos x}{2}}$ $\tan\left(\frac{x}{2}\right) = \frac{1 - \cos x}{\sin x} = \frac{\sin x}{1 + \cos x}$
<p>Sum – to - Product Formulas</p> $\sin x + \sin y = 2\sin\left(\frac{x+y}{2}\right)\cos\left(\frac{x-y}{2}\right)$ $\sin x - \sin y = 2\cos\left(\frac{x+y}{2}\right)\sin\left(\frac{x-y}{2}\right)$ $\cos x + \cos y = 2\cos\left(\frac{x+y}{2}\right)\cos\left(\frac{x-y}{2}\right)$ $\cos x - \cos y = -2\sin\left(\frac{x+y}{2}\right)\sin\left(\frac{x-y}{2}\right)$	<p>Product – to - Sum Formulas</p> $2\sin x \cos y = \sin(x+y) + \sin(x-y)$ $2\cos x \sin y = \sin(x+y) - \sin(x-y)$ $2\cos x \cos y = \cos(x+y) + \cos(x-y)$ $2\sin x \sin y = \cos(x-y) - \cos(x+y)$
<p>Area of a Triangle</p> <div style="text-align: center;">  </div> $A = \frac{1}{2}ab \sin C$	<p>Law of Sines</p> $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$ <p>Law of Cosines</p> $a^2 = b^2 + c^2 - 2bc \cos A$ $b^2 = a^2 + c^2 - 2ac \cos B$ $c^2 = a^2 + b^2 - 2ab \cos C$

The Trigonometric Functions

In a right triangle:

Hypotenuse is the side opposite of the right angle and always is the *longest* side.

Adjacent is the side next to the angle θ . **Opposite** is the side opposite of the angle θ

$$\sin \theta = \frac{opp}{hyp}$$

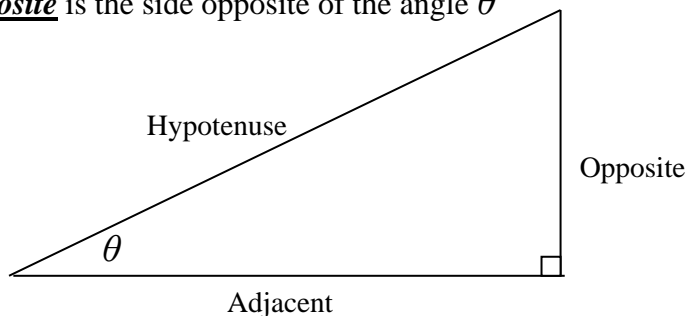
$$\csc \theta = \frac{hyp}{opp}$$

$$\cos \theta = \frac{adj}{hyp}$$

$$\sec \theta = \frac{hyp}{adj}$$

$$\tan \theta = \frac{opp}{adj}$$

$$\cot \theta = \frac{adj}{opp}$$



Note: The function in the second column is the reciprocal of the function in the first column.

Unit Circle

Note: Any point along the unit circle has an x-coordinate whose value is equal to the cosine of the angle and a y-coordinate whose value is equal to the sine of the angle.

Special Triangles

